

# Simplifying the martian carbon dioxide cycle: An empirical method for predicting surface pressure

Paul Withers<sup>1</sup>, Silvia Tellmann<sup>2</sup>

1 - Boston University

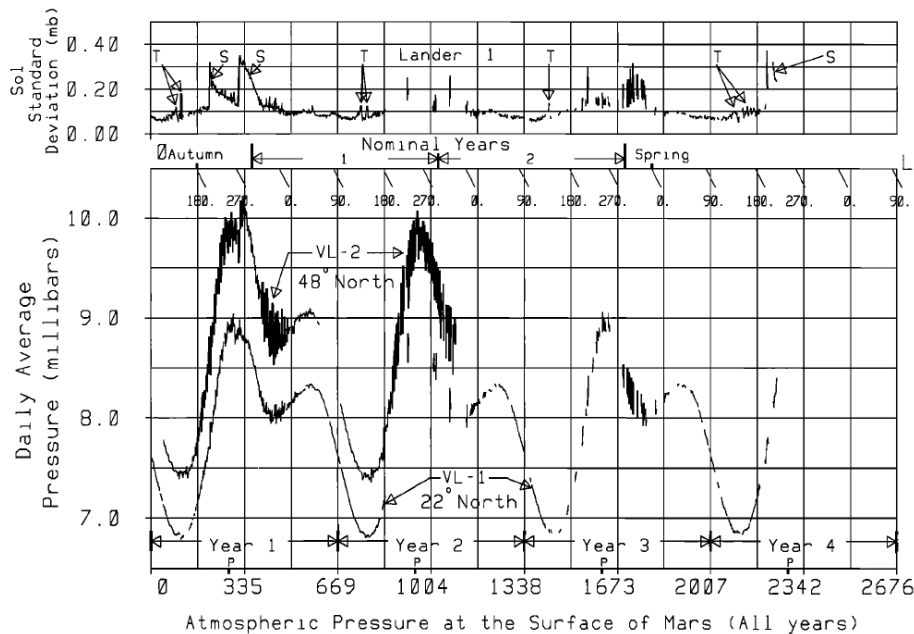
2 – Rheinisches Institut für Umweltforschung,  
Cologne, Germany  
(withers@bu.edu)

Thursday 2009.07.23 17:30

Third International Workshop on Mars Polar  
Energy Balance and the CO<sub>2</sub> Cycle,  
Seattle, WA

# Background

Viking Lander pressure data  
Fig 1 of Tillman et al. (1993)



- Martian surface pressure exhibits significant spatial and temporal variations
- Accurate predictions of surface pressure have a range of applications, including
  - Polar energy balance studies
  - Geodetic studies of rotation state and gravity field
  - Derivation of absolute altitude scales for T(p) profiles
  - Landing site evaluations
- Objective is to find a simple empirical expression that can predict diurnal-mean surface pressure
  - Ease of application, transparency desired
  - Minimize use of complicated models
  - Validate against observations
- Optimize for MSL landing conditions (Ls=120 to 180, z<+1 km, 45S to 45N), but desire adequate predictions for all conditions

# Available Datasets

- LANDERS
- VL1
  - Multiple years, coarse digitization, 22N
- VL2
  - Almost one year, coarse digitization, 48N
- MPF
  - Ls=142-188, same elevation as VL1, systematic error of about 0.1 mbar, 19N
- PHX
  - Ls=76-151, 68N, large and precise dataset
  - Data from Ls=120 to 151 not yet incorporated into analysis
- RADIO OCCULTATIONS
- Mariner 9
  - Apparent inconsistencies of 10%
- VO1 and VO2
  - Barely 20 pressures reported
- MGS
  - 21243 profiles, including 297 at Ls=120-180,  $z < +1$  km, latitude=45S to 45N
  - Extrapolate  $p(r)$  to MOLA surface and assign MOLA altitude
- MEX
  - 484 profiles, only 5 at Ls=120-180,  $z < +1$  km, latitude=45S to 45N

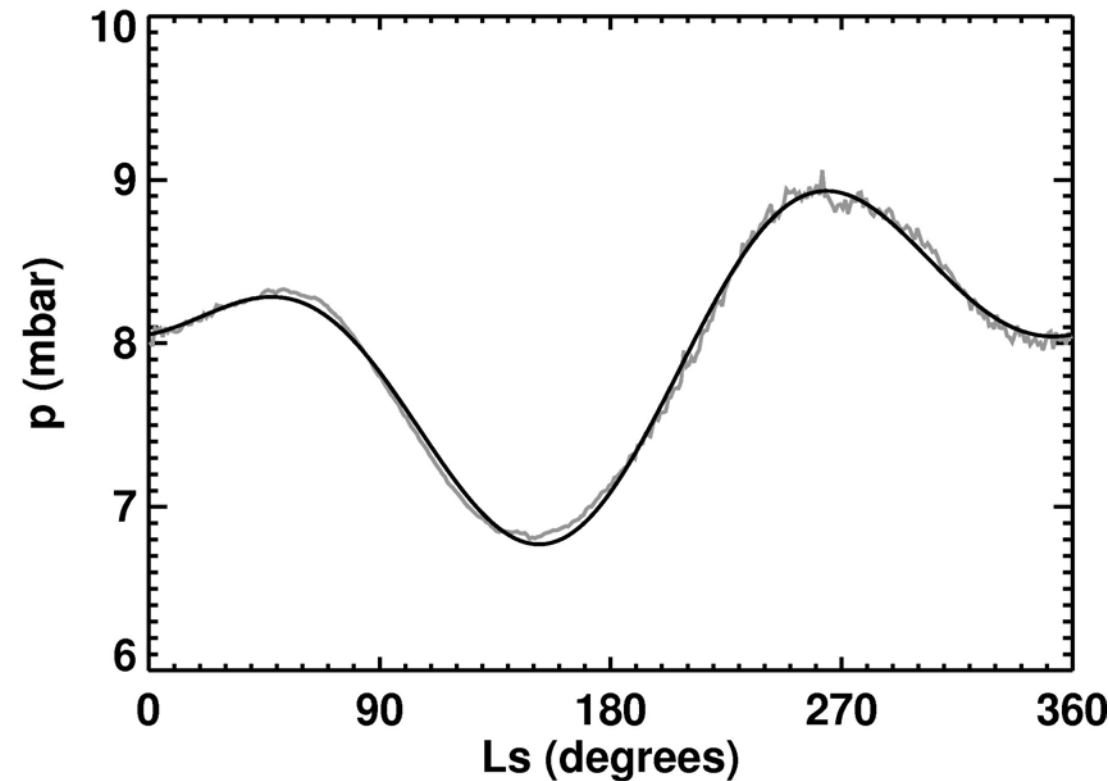
Most useful datasets are: VL1 for seasonal cycle, MGS for validation and testing,

Goal is: Simple expression for DIURNAL MEAN Ps as function of season and altitude.

# Approach

Grey line is 360 diurnal mean surface pressure from VL1

Black line is wave-2 fit



Use expression below to predict surface pressure,  $P_s$   
 $z_{VL1} = -3.63$  km  
Constant and uniform  $H_0$  needed (found on next slide)

Parameter	VL1
$p_0$ (mbar)	7.9723740
$s_1$	-0.068622849
$c_1$	0.060390972
$s_2$	0.044663631
$c_2$	-0.050183946

$$p_s = p_{0,VL1} \exp(-(z - z_{VL1})/H_0) \times \text{Eqn 1}$$

$$(1 + s_{1,VL1} \sin(1L_s) + c_{1,VL1} \cos(1L_s) + s_{2,VL1} \sin(2L_s) + c_{2,VL1} \cos(2L_s))$$

Optimize with Delta metric, where  $\Delta = (p_{\text{pred}} - p_{\text{meas}}) / p_{\text{meas}}$

# Finding H0 from MGS

- Quickly find that  $H_0 < 10$  km and  $H_0 > 12$  km have problems at low and high altitudes
- MGS measurements at  $z < +1$  km and 45S to 45N divide neatly into seven  $L_s$  blocks

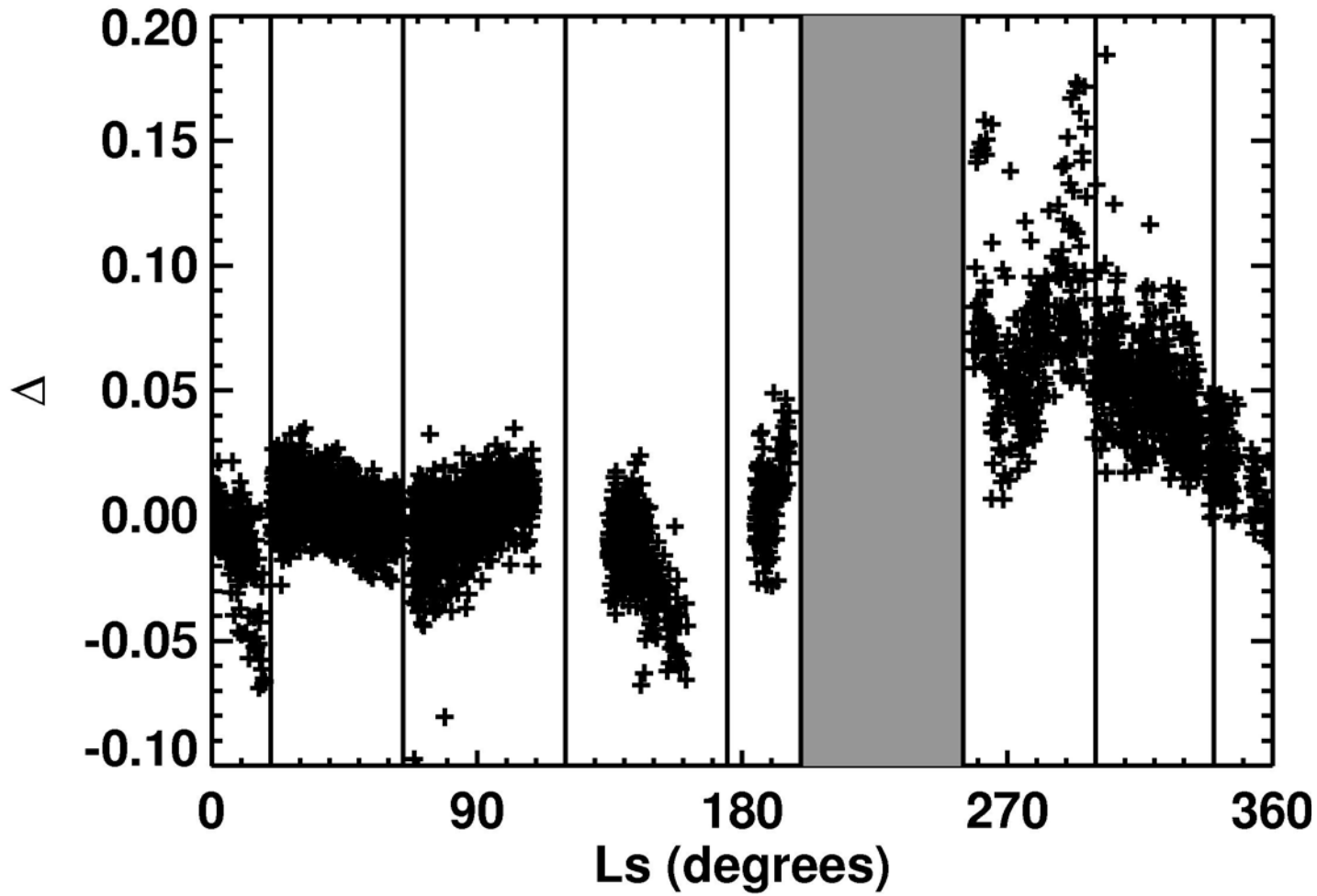
$L_s$ range	N	$\bar{z}$ (km)	$H_0$ (km)	$\bar{\Delta}$	S. D. of $\Delta$
340°–20°	293	-1.3	10.0	-2.1E-02	3.2E-02
			10.5	-9.9E-03	2.5E-02
			11.0	1.5E-04	2.3E-02
			11.5	9.5E-03	2.6E-02
			12.0	1.8E-02	3.2E-02
20°–65°	824	-2.9	10.0	-4.1E-03	1.5E-02
			10.5	-8.5E-04	1.0E-02
			11.0	2.2E-03	1.0E-02
			11.5	5.1E-03	1.4E-02
			12.0	7.7E-03	1.9E-02
65°–120°	740	-2.2	10.0	-1.4E-02	1.9E-02
			10.5	-7.2E-03	1.5E-02
			11.0	-1.1E-03	1.4E-02
			11.5	4.6E-03	1.6E-02
			12.0	9.9E-03	1.9E-02
120°–175°	297	-1.7	10.0	-3.4E-02	2.6E-02
			10.5	-2.5E-02	2.1E-02
			11.0	-1.7E-02	1.8E-02
			11.5	-9.7E-03	1.7E-02
			12.0	-2.9E-03	1.8E-02

$L_s$ range	N	$\bar{z}$ (km)	$H_0$ (km)	$\bar{\Delta}$	S. D. of $\Delta$
175°–200°	127	-2.8	10.0	-2.2E-04	1.9E-02
			10.5	3.7E-03	1.6E-02
			11.0	7.3E-03	1.6E-02
			11.5	1.1E-02	1.8E-02
			12.0	1.4E-02	2.1E-02
255°–300°	306	-1.0	10.0	4.8E-02	4.4E-02
			10.5	6.1E-02	3.7E-02
			11.0	7.3E-02	3.2E-02
			11.5	8.3E-02	2.9E-02
			12.0	9.4E-02	2.7E-02
300°–340°	479	-1.3	10.0	2.6E-02	2.9E-02
			10.5	3.8E-02	2.3E-02
			11.0	4.8E-02	2.0E-02
			11.5	5.8E-02	2.0E-02
			12.0	6.7E-02	2.3E-02

Optimal  
scale  
height is:

$H_0 = 11$  km  
Equivalent  
to  $T=215$  K,  
which is  
reasonable

# Delta vs Ls for MGS



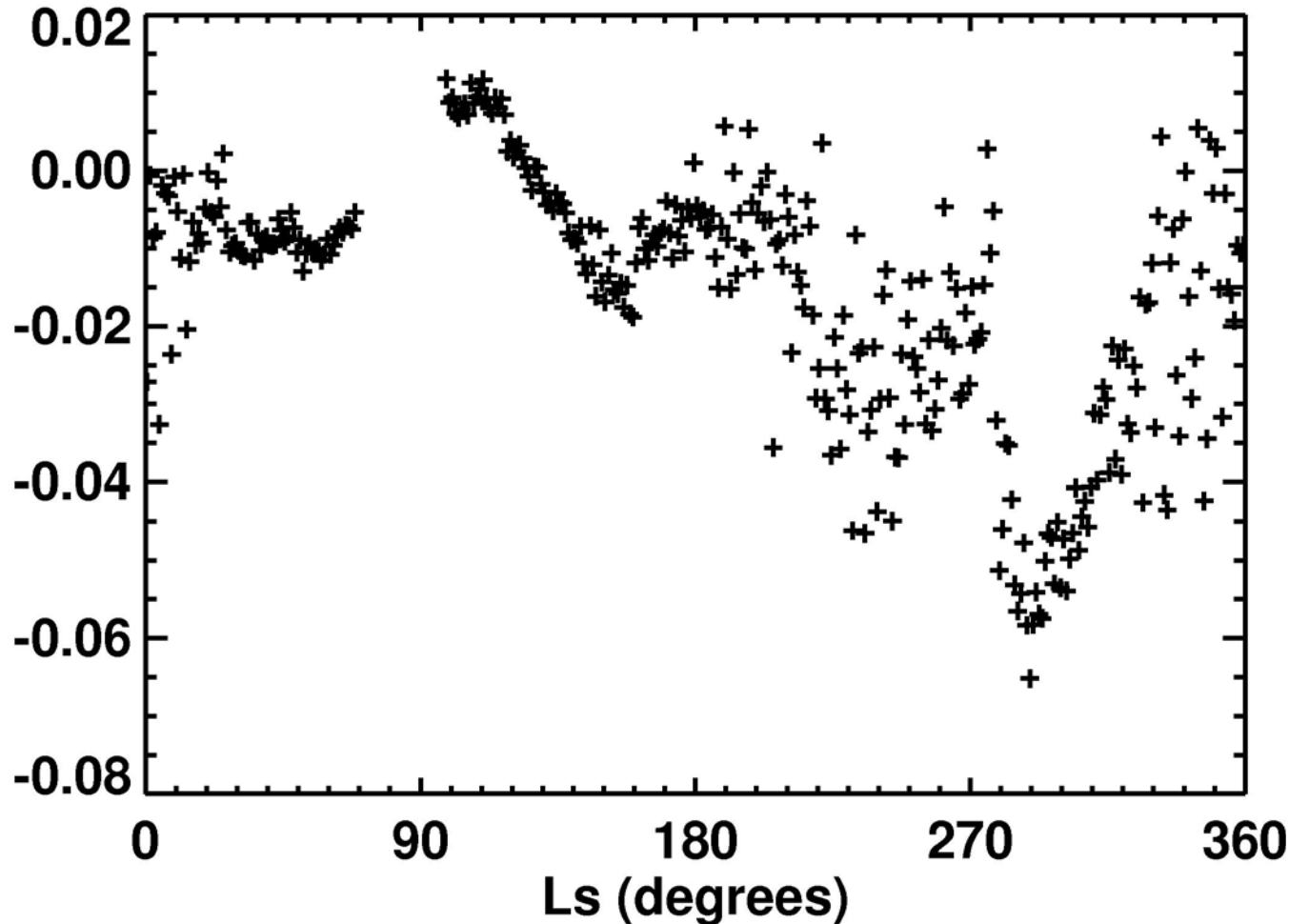
Poor predictions  
at Ls=255-340

OK at other  
seasons

Possible trend  
with Ls at  
Ls=120-175?

Only data from  $z < +1$  km and 45S to 45N shown here

# Delta vs Ls for VL2



Poor predictions  
at Ls=240-360

OK at other  
seasons

Trend with Ls at  
Ls=110-160,  
similar to MGS?

Going to wave-4 in  
 $f(Ls)$  fixes this trend  
in VL1 and VL2, but  
has no effect on  
trend in MGS

So retain wave-2  
for  $f(Ls)$

# Accuracy of Predictions

Mission	$\bar{\Delta}$	S. D. of $\Delta$	$\bar{\Delta}$	S. D. of $\Delta$
	(all $L_s$ )	(all $L_s$ )	( $L_s = 120^\circ-180^\circ$ )	( $L_s = 120^\circ-180^\circ$ )
VL1	2.5E-3%	0.6%	-0.4%	0.6%
VL2	6.7E-3%	1.1%	-0.4%	0.6%
MPF	2.2%	0.2%	2.2%	0.2%
PHX	-0.2%	3.0%	—	—
MGS	1.4%	3.2%	-1.7%	1.8%
MEX	0.2%	3.3%	-7.1%	7.0%

**Expect 3% accuracy for MSL landing  
with 1-sigma confidence level**

Overbar = Mean

S. D. = Standard deviation

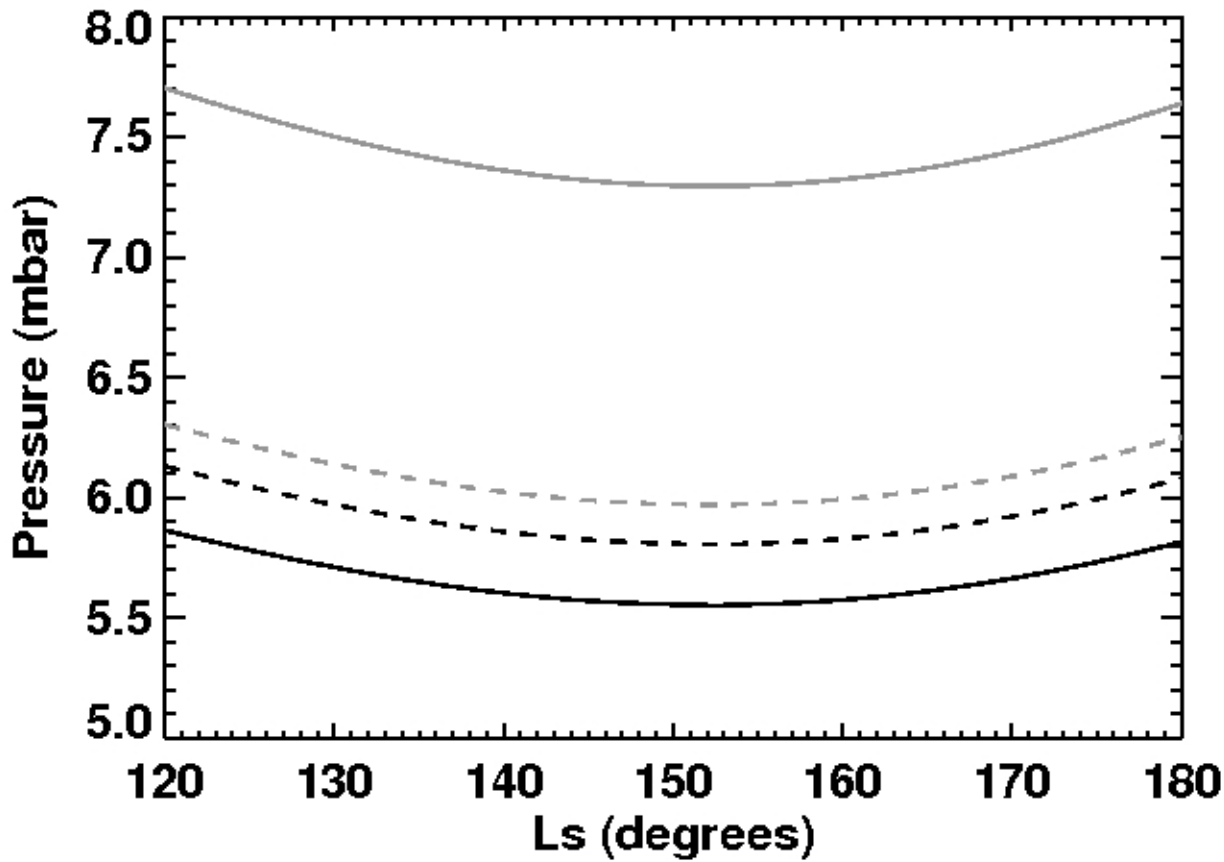
Only data from  $z < +1$  km and 45S to 45N used for orbital datasets



# Evaluation

- Data from VL1 and MGS were used to obtain predictive expression, so good predictions for these data should not be over-interpreted
- However, MGS data do span a very wide range of altitudes, latitudes, and longitudes
- VL2 results are encouraging
- MPF surface pressures are systematically too small by  $\sim 0.1$  mbar, as noted by previous workers (Haberle et al., 1999) due to problems in pre-flight testing. Standard deviation of Delta is reassuringly small.
- PHX results are encouraging, especially coming from 68N, which is far north of the VL1 site at 22N
- MEX results at  $L_s=120$  to 180 are influenced by “small number statistics” (5 profiles). Also, preliminary versions of MEX profiles were used here. Results improve when final versions are used.

# Predictions for MSL



Eberswalde (-1.450 km)  
Solid black line  
23.86S, 326.73E

Gale (-4.451 km)  
Solid grey line  
4.49S, 137.42E

Holden (-1.940 km)  
Dashed black line  
26.37S, 325.10E

Mawrth (-2.246 km)  
Dashed grey line  
24.01N, 341.03E

# Potential Applications

- First-order surface pressure estimates for landing site selection
- Reality-check on predictions from more complex, physics-based models
- Total atmospheric mass from Eqn 1 is about  $10 p_0 R^2 f(L_s) / g$ . Annual mean value is  $2.4E16$  kg and difference between maximum and minimum values is  $6.6E15$  kg, consistent with previous results.
- Correct orbital gamma ray and neutron spectrometer for atmospheric absorption effects
- Absolute altitude scales for  $T(p)$  profiles measured from orbit, such as MGS TES or Mariner 9 IRIS profiles
- Theoretical simulations of dust lifting and aeolian modification of surface features, the thermodynamic stability of near-surface liquids, and the surface radiation environment

# Conclusions

- A simple expression with 7 free parameters provides surprisingly accurate predictions for surface pressure
- Expected accuracy of prediction for MSL landing is 3% (1-sigma confidence level)
- Predictions are least accurate at  $L_s=240$  to 360 when interannual variability (large dust storms) is greatest
- There are many potential applications for accurate surface pressure predictions